

1. [8 points] Consider the function

$$f(x) = 2x^3 + 5x.$$

Find an equation for the tangent line to the graph $y = f(x)$ at the point where $x = -1$.

2. [24 points] Evaluate the derivative of each function. You **do not need to simplify** your answers.

(a) $\frac{2x + 1}{3x + 1}$

(b) $\frac{2x^2 + 3\sqrt{x} + 5}{\sqrt{x}}$

(c) $\sqrt{3 + (1 + x)^4}$

(d) $\frac{(2 + 3x)^2}{\sqrt{3 - x}}$

3. [8 points] Let

$$f(x) = \sqrt{1 + x^2}.$$

Use the **limit definition** of the derivative to find $f'(x)$.

4. [12 points] Consider the function

$$f(x) = \frac{x^2 + 1}{2x + 1}.$$

(a) Compute **and simplify** the derivative $f'(x)$.

(b) Compute **and simplify** the second derivative $f''(x)$. Your final answer should be $\frac{10}{(2x + 1)^3}$.

For full credit, show each step of your simplification.

5. [8 points] At what points is the tangent line to the graph $y = (x + 1)^2(2x - 1)^3$ horizontal? For this problem, **it is enough to state the x -coordinate only** in your answer.

6. [3 points (bonus)] Evaluate and simplify

$$\frac{d}{dx} \sqrt{1 + (5 + \sqrt{x/6})^{12}}.$$